

4.3 Solving Equations Literally

A Practice Understanding Task

try the left side

Solve each of the following equations for x :

$$1. \frac{3x+2}{5} = 7$$

$$2. \frac{3x+2y}{5} = 7 \cdot 5$$

$$\cancel{3x+2y} = 35$$

$$-2y \quad -2y$$

$$\frac{3x}{3} = \frac{35-2y}{3}$$

$$3. \frac{4x}{3} - 5 = 11$$

$$4. \frac{4x}{3} - \frac{5y}{3} = 11$$

$$+5y \quad +5y$$

$$\cancel{\frac{4x}{3}} = 11 + 5y$$

$$5. \frac{2}{5}(x+3) = 6$$

$$\cancel{5} \cdot \frac{2}{5}(x+y) = 6 \cdot 5$$

$$7. 2(3x+4) = 4x + 12$$

$$\cancel{2}(x+y) = 30$$

$$\cancel{x} \quad \cancel{y}$$

$$x+y = 15$$

$$\cancel{-x} \quad \cancel{-y}$$

Write a **verbal description** for each step of the equation solving process used to solve the following equations for x . Your description should include statements about how you know what to do next. For example, you might write, "First I _____ because _____..."

Solve for X

$$9. \frac{ax+b}{c} - d = e$$

ADD D
Multiply C
Subtract B
Divide A

$$10. r \cdot \sqrt{\frac{mx}{n} + s} = t$$

Divide R
Square both sides
Subtract S
Multiply N
Divide M

Solve each equation for x. Provide the justifications for each step. See the first example as a reminder for the types of justifications that might be used.

Example:

$$\begin{array}{rcl} 3x - 6 & = & 15 \\ +6 \quad +6 & & \\ \hline 3x & = & 21 \\ \frac{3x}{3} & = & \frac{21}{3} \\ x & = & 7 \end{array}$$

	Justification
Addition Property of equality	
Division Property of equality	

11.

$$\begin{array}{rcl} 4x - 10 & = & 2 \\ +10 \quad +10 & & \\ \hline 4x & = & 12 \\ \frac{4x}{4} & = & \frac{12}{4} \\ x & = & 3 \end{array}$$

	Justification
Addition Prop	
Division Prop	

12.

$$\begin{array}{rcl} 6x + 3 & = & x + 18 \\ -x \quad -x & & \\ \hline 5x + 3 & = & 18 \\ -3 \quad -3 & & \\ \hline 5x & = & 15 \\ \frac{5x}{5} & = & \frac{15}{5} \\ x & = & 3 \end{array}$$

	Justification
Subtraction Prop	
Subtraction Prop	
Division Prop	

13.

$$\begin{array}{rcl} 3x - 10 & = & 2x + 12 \\ +10 \quad +10 & & \\ \hline 3x & = & 2x + 22 \\ -2x \quad -2x & & \\ \hline x & = & 22 \end{array}$$

	Justification
Addition Prop	
Subtraction Prop	

14.

$$\begin{array}{rcl} 12x + 3y & = & 15 \\ -3y \quad -3y & & \\ \hline 12x & = & 15 - 3y \\ \frac{12x}{12} & = & \frac{15 - 3y}{12} \\ x & = & \frac{5}{4} - \frac{1}{4}y \end{array}$$

	Justification
Subtraction Prop	
Division Prop	

15.

$$\begin{array}{rcl} x(b + 7) & = & 9 \\ b + 7 \quad b + 7 & & \\ \hline x & = & \frac{9}{b+7} \end{array}$$

	Justification
Division	

$$3) \text{ Solve for } x \\ 3x + y = z \quad x = \frac{z-y}{3} \text{ or } \frac{z}{3} - \frac{y}{3}$$

Solve for d

$$11) \quad 4d - p = m \quad d = \frac{m+p}{4} \text{ or } \frac{m}{4} + \frac{p}{4}$$

14) Solve for v

$$\frac{1}{5}v + gt = a \quad v = 5(a-gt)$$

~~gt~~ - gt

$$5 \cdot \frac{1}{5}v = (a-gt)5 \quad v = 5a - 5gt$$

16) Solve for x

$$nxz - f = 3f \quad x = \frac{4f}{nz}$$

4) Solve for d

$$q + ad = m \quad d = \frac{m-q}{a} \quad \frac{m}{a} - \frac{q}{a}$$

Solve for w

$$13) \quad 24 = l \cdot w \cdot h \quad w = \frac{24}{lh}$$

Solve for r

$$8rs - 8s = 16p$$

~~8s~~ + 8s + 8s

$$2) \quad \frac{8rs}{8s} = \frac{16p}{8s} + \frac{8s}{8s} \quad \boxed{r = \frac{2p}{s} + 1}$$

Solve for d

$$6) \quad fd - m = 8 \quad d = \frac{8+m}{f} \quad \frac{8}{f} + \frac{m}{f}$$

Solve for g

$$10) \quad 2g - 4f = 6f \quad g = 5f$$

Solve for w

$$15) \quad 2wy - 8n = 4k \quad w = \frac{2k + 8n}{y}$$

$$7) \quad 2wy = 4k + 8n$$

Solve for c $p = 4c$

Solve for g

$$bg + 9f = 27$$