

Complete the square to solve for x.

Warmup

$x^2 - 14x - 12 = 0$

$3x^2 - 12x + 1 = 0$

$x^2 + x - 10 = 0$

Now we are going to complete the square and leave it in vertex form.

** **Vertex form:** $y = a(x - h)^2 + k$ standard \rightarrow vertex

$y = x^2 + 10x + 15$

$x^2 + 10x + 15 = 0$

$-15 \quad -15$

$x^2 + 10x + \frac{25}{2} = \frac{-15 + 25}{2}$

$(5)^2 = 25$

$(x+5)(x+5) = 10$

$(x+5)^2 = 10$

$-10 \quad -10$

$(x+5)^2 - 10 = 0$

Vertex: $(-5, -10)$ Max or Min: Min

$y = x^2 - 8x - 4$

$x^2 - 8x - 4 = 0$

$+4 \quad +4$

$x^2 - 8x + 16 = 4 + 16$

$(-4)^2 = 16$

$(x-4)(x-4) = 20$

$(x-4)^2 = 20$

$-20 \quad -20$

$(x-4)^2 - 20 = 0$

Vertex: $(4, -20)$ Max or Min: Min

$$y = 2x^2 + 12x + 17$$

$$2x^2 + 12x + 17 = 0$$

$$\begin{array}{r} -17 \quad -17 \\ 2x^2 + 12x = -17 \\ \hline \quad \quad \hline \end{array}$$

$$2\left(x^2 + \frac{6x}{2} + \frac{9}{2}\right) = -17 + \frac{2(9)}{2}$$

$$(3)^2 = 9$$

$$2(x+3)(x+3) = 1$$

$$2(x+3)^2 = 1$$

$$2(x+3)^2 - 1 = 0$$

Vertex: $(-3, -1)$ Min or Max: Min

$$y = \frac{1}{2}x^2 - 6x + 11$$

$$\frac{1}{2}x^2 - 6x + 11 = 0$$

$$\begin{array}{r} -11 \quad -11 \\ \frac{1}{2}x^2 - 6x = -11 \\ \hline \quad \quad \hline \end{array}$$

$$\frac{1}{2}\left(x^2 - \frac{12x}{2} + \frac{36}{2}\right) = -11 + \frac{1}{2}(36)$$

$$(-6)^2 = 36$$

$$\frac{1}{2}(x-6)^2 = 7$$

$$\frac{1}{2}(x-6)^2 - 7 = 0$$

Vertex: $(6, -7)$ Min or Max: Min

$$y = -4x^2 - 64x - 156$$

$$-4x^2 - 64x - 156 = 0$$

$$\begin{array}{r} +156 \quad +156 \\ -4x^2 - 64x = 156 \\ \hline \quad \quad \hline \end{array}$$

$$-4\left(x^2 + \frac{16x}{2} + \frac{64}{2}\right) = 156 + \frac{-4(64)}{2}$$

$$(8)^2 = 64$$

$$-4(x+8)^2 = -100$$

$$-4(x+8)^2 + 100 = 0$$

Vertex: $(-8, 100)$ Min or max: Max

$$y = -x^2 + 4x - 10$$

Vertex: _____ Min or Max: _____

$x^2 - 12x + 32 = 0$
 $x^2 - 12x + \frac{36}{2} = -32 + \frac{36}{2}$
 $(-6)^2 = 36$
 $(x-6)^2 = 4$
 $-4 - 4$
 $(x-6)^2 - 4 = 0$

Vertex: $(6, -4)$ Min or Max: Min

$y = -2x^2 - 12x + 8$
 $-2x^2 - 12x + 8 = 0$
 $-2x^2 - 12x = -8$
 $\frac{-2}{-2} \frac{-12}{-2} = \frac{-8}{-2} + \frac{-2(9)}{-2}$
 $(-2)(x^2 + 6x + 9) = -8 + -2(9)$
 $(3)^2 = 9$
 $-2(x+3)^2 = -8 - 18$
 $+26 + 26$
 $-2(x+3)^2 + 26 = 0$

Vertex: $(-3, 26)$ Min or Max: Max

Let's look at these special cases for complete the square.

$x^2 + 4x + 4 = 0$
 $x^2 + 4x + \frac{4}{2} = -10 + \frac{4}{2}$
 $(2)^2 = 4$
 $(x+2)(x+2) = -6$
 $\sqrt{(x+2)^2} = \sqrt{-6}$
** Cannot take square root of a negative*
No Solution

$x^2 - 10x + 25 = 0$
 $x^2 - 10x + \frac{25}{2} = -65 + \frac{25}{2}$
 $(-5)^2 = 25$
 $(x-5)^2 = -40$
 $\sqrt{(x-5)^2} = \sqrt{-40}$
No Solution

$-3x^2 + 12x - 21 = 0$
 $\frac{-3}{-3} x^2 + \frac{12}{-3} x = \frac{21}{-3}$
 $(-3)(x^2 - 4x + 4) = 21 + -3(4)$

$(-2)^2 = 4$
 $\sqrt{(x-2)^2} = \sqrt{-3}$
No Solution

(HW) (TOP) Vertex form, Vertex, Max/Min

① $y = x^2 - 4x + 10$

$x^2 - 4x + 10 = 0$
 $-10 \quad -10$

$x^2 - \frac{4x}{2} + \frac{4}{2} = -10 + 4$

$(-2)^2 = 4$

$(x-2)(x-2) = -6$

$(x-2)^2 = -6 + 4$

$(x-2)^2 + 6 = 0$

Min Vertex
(2, 6)

Middle complete the [] to solve

⑧ $\frac{9x^2}{9} - \frac{81x}{9} = 12$

$9(x^2 - 9x + 20.25) = 12 + 9(20.25)$

$(-4.5)^2 = 20.25$

$9(x-4.5)^2 = \frac{194.25}{9}$

$\sqrt{(x-4.5)^2} = \sqrt{\frac{259}{12}}$

$x-4.5 = \pm \sqrt{\frac{259}{12}}$
 $+4.5 \quad +4.5$

$x = 4.5 \pm \sqrt{\frac{259}{12}}$

Factor

$\frac{4x^2}{4} - \frac{16}{4}$

$4(x^2 - 4)$
 $x \quad x \quad 2 \quad -2$

$4(x-2)(x+2)$

$4x^2 - 4x - 3$
 -12
 $-6 \quad 2$

	$2x$	-3
$2x$	$4x^2$	$-6x$
1	$2x$	-3

$(2x-3)(2x+1)$

$-\frac{6}{4} \quad \frac{2}{4}$
 $-\frac{3}{2} \quad \frac{1}{2}$

$(2x-3)(2x+1)$