

Exponentials have two graphs, **GROWTH** and **DECAY**.



ALL OF THESE GRAPHS START AT (0, 1)!

GROWTH

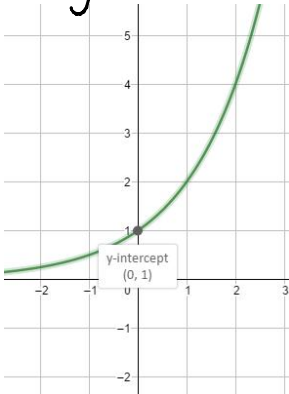
PARENT GRAPH

Asymptote: $y=0$

$y = 2^x$

y-int: (0, 1)

2 → base
> 1
growth

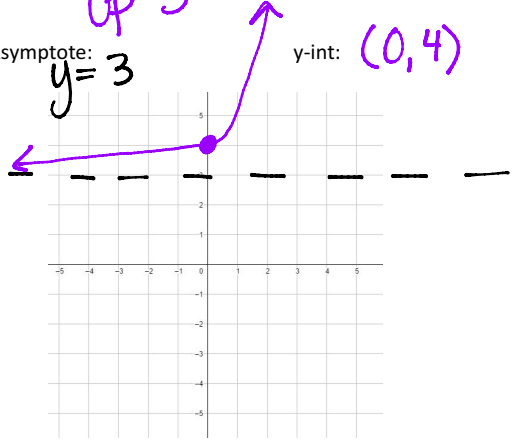


$y = 2^x + 3$

How do we move?

UP 3
Asymptote: $y=3$

y-int: (0, 4)



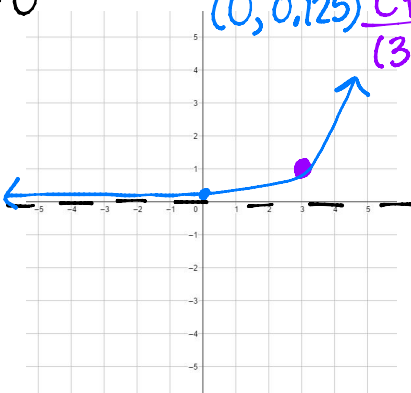
$y = 2^{(x-3)}$

How do we move?

Right 3

Asymptote: $y=0$

y-int: (0, 0.125) CP (3, 1)



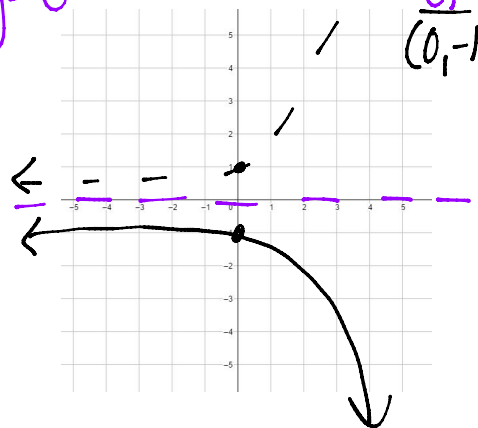
$y = -1(2)^x$

How do we move?

Reflect over X-axis

Asymptote: $y=0$

y-int: (0, -1) CP (0, -1)



How do we move?

$$y = 4(2)^x$$

Vertical stretch

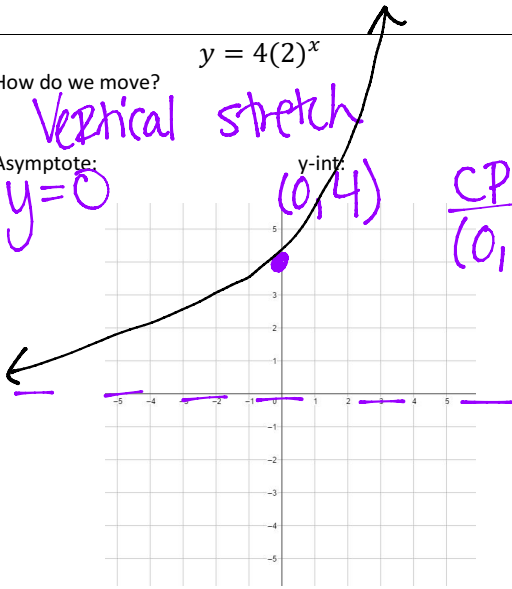
Asymptote:

$$y = 0$$

y-int:

$$(0, 4)$$

$$\text{CP} \\ (0, 4)$$



How do we move?

$$y = \frac{1}{2}(2)^x$$

Horiz-stretch

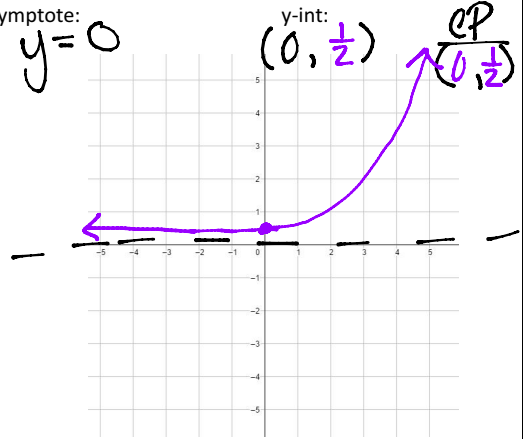
Asymptote:

$$y = 0$$

y-int:

$$(0, \frac{1}{2})$$

$$\text{CP} \\ (0, \frac{1}{2})$$



How do we move?

$$y = 2^{(x+2)} - 2$$

left 2 Down 2

$$2^{0+2} - 2$$

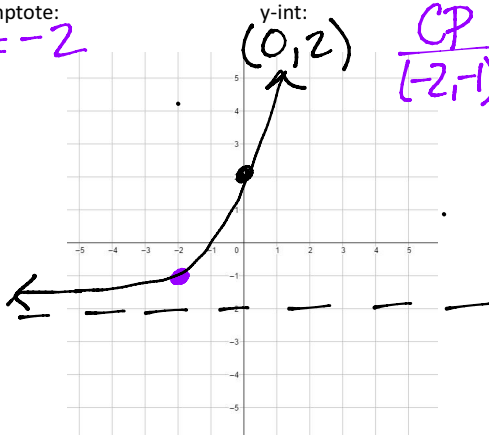
Asymptote:

$$y = -2$$

y-int:

$$(0, 2)$$

$$\text{CP} \\ (-2, -1)$$



How do we move?

$$y = 3(2)^x - 4$$

Vertical stretch

Down 4

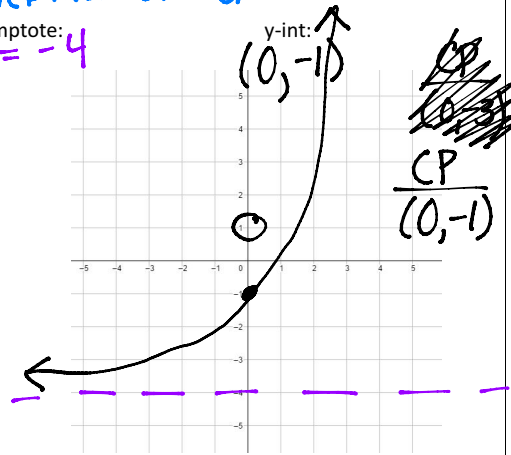
Asymptote:

$$y = -4$$

y-int:

$$(0, -1)$$

$$\text{CP} \\ (0, -1)$$



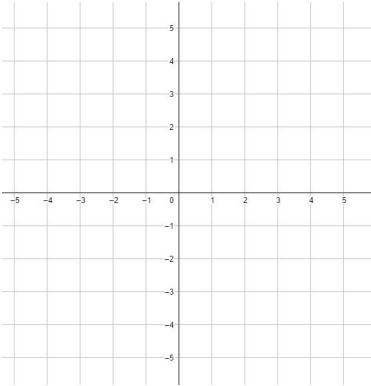
DECAY

$$y = \frac{1}{2}^x - 4$$

How do we move?

Asymptote:

y-int:

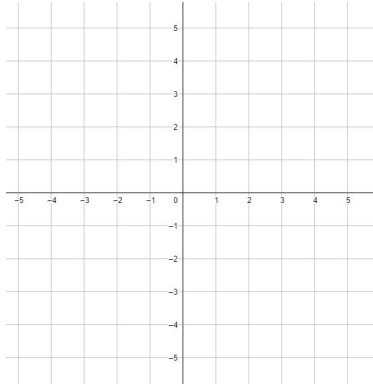


$$y = \frac{1}{2}^{(x+3)}$$

How do we move?

Asymptote:

y-int:

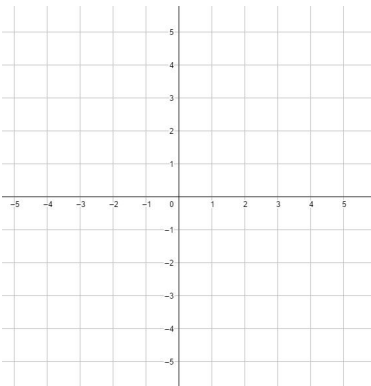


$$y = 2\left(\frac{1}{2}\right)^x - 2$$

How do we move?

Asymptote:

y-int:

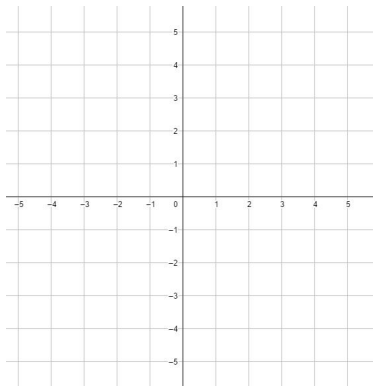


$$y = -\left(\frac{1}{2}\right)^x$$

How do we move?

Asymptote:

y-int:



- When you are in the exponent, you move _____ or _____ (think opposite)
- When you are in the back of the equation (_____) you move _____ or _____
- **BIG DIFFERENCE BETWEEN GROWTH AND DECAY IS**

Write the equations for the following specific scenarios.

- 1) An exponential growth that has been shifted right 5 units and down 3 units.
- 2) A quadratic that has been reflected over the x-axis and left 3 units.
- 3) An exponential decay that has been vertically stretch by a factor of 10.
- 4) An exponential growth that has an asymptote of 4 and moved right 2 units.
- 5) A quadratic that has been horizontally stretched by $\frac{1}{4}$ and moved down 6 units.
- 6) A line that has a slope of 10 and a y-intercept of 2.
- 7) An exponential decay that has been vertically shrunk by a factor of $\frac{1}{6}$ and reflected over the x-axis.
- 8) An exponential growth that has been moved left 8 units and has an asymptote of -4.