

Let's look at the following system: $\begin{cases} 3t + 4f = 43 \\ 3t + 6f = 54 \end{cases}$

We need to solve it but for each step, we are going to label (explain) what we are doing along the way. In a way, we are going to set up a strategy to help us solve each system from here on out. Be sure that you write clearly so that if you were to pass this to your neighbor, or HEAVEN FORBID your parents saw this, they could read what you wrote down.

Problem	What is going on?
$\begin{array}{r} -1(3t + 4f = 43) \\ 3t + 6f = 54 \\ \hline -3t - 4f = -43 \\ \hline 2f = 11 \\ \frac{2f}{2} = \frac{11}{2} \\ f = 5.5 \end{array}$ $3t + 4(5.5) = 43$ $\begin{array}{r} 3t + 22 = 43 \\ -22 \quad -22 \\ \hline 3t = 21 \\ \frac{3t}{3} = \frac{21}{3} \\ t = 7 \end{array}$ $(7, 5.5)$	<p>① Multiply top eq. by -1 to eliminate t</p> <p>② Add like terms</p> <p>③ Divide</p> <p>④ Plug f in to solve for t</p> <p>⑤ Subtract</p> <p>⑥ Divide</p> <p>⑦ Make point</p>

As you were going through this problem, did your mindset match what we wrote down on the right hand side?

Do you stop when you find one answer? Why or why not?

No, you need a point (x, y)

Is it necessary to show all your work? Why?

Yes, make Boo Boo you can fix it.

Now try these two problems explaining each along the way.

Problem	What is going on?
$\begin{cases} 2x + 3y = 42.50 \\ 5x + 6y = 94.25 \end{cases}$ $\begin{array}{r} -5 \\ 2 \end{array} \begin{cases} 2x + 3y = 42.50 \\ 5x + 6y = 94.25 \end{cases}$ $\begin{array}{r} -10x - 15y = -212.5 \\ 10x + 12y = 188.5 \end{array}$ $\begin{array}{r} -3y = -24 \\ \underline{-3} \quad \underline{-3} \\ y = 8 \end{array}$ $2x + 3(8) = 42.5$ $2x + 24 = 42.5$ $\begin{array}{r} -24 \quad -24 \\ 2x = 18.5 \\ \underline{2} \quad \underline{2} \\ x = 9.25 \end{array} \quad (9.25, 8)$	<ol style="list-style-type: none"> 1) Multiply top by -5 2) Multiply bottom by 2 3) Add like terms 4) divide 5) plug in y to solve for x 6) subtract 7) divide 8) Make point

Problem	What is going on?
$\begin{cases} 2b + 4t = 18.50 \\ 2b - 3t = 1.00 \end{cases}$	$(4.25, 2.5)$

Let's look at a **graph**. Carlos thinks that when he graphs the two systems, he can show the cost of each item on the graph.

- Carlos purchased 6 dog leashes and 6 cat brushes for \$45.00 for Clarita to use while pampering the pets. Later in the summer he purchased 3 additional dog leashes and 2 cat brushes for \$19.00. Based on the information given, figure out the price of each item.

$x = \text{leashes}$
 $y = \text{brushes}$

$$6x + 6y = 45$$

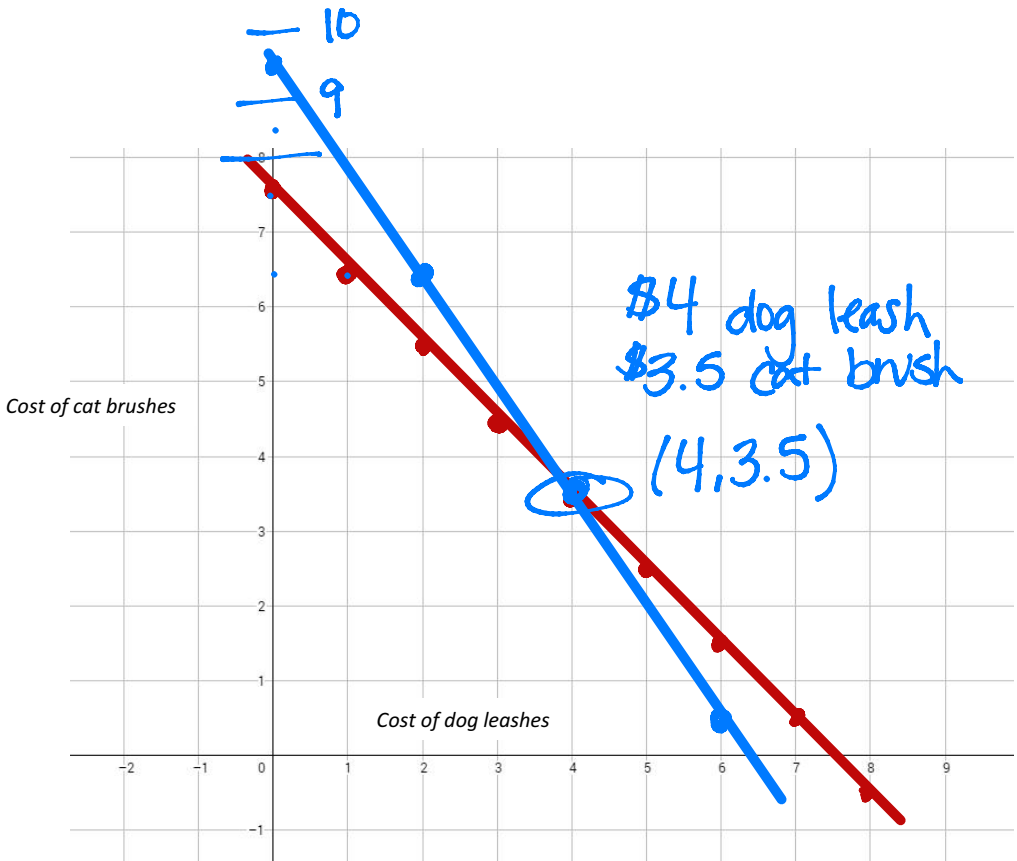
$$y = -x + 7.5$$

$$y = -x + 7.5$$

$$3x + 2y = 19$$

$$y = -\frac{3}{2}x + 9.5$$

$$y = -\frac{3}{2}x + 9.5$$



Now try this word problem. Reread it to be sure you have all the information.

- A 150 yard pipe is cut to provide drainage for two fields. If the length of the one piece (a) is three yards less than twice the length of the second piece (b), what are the lengths of the two pieces?

$$\begin{array}{l}
 a = \text{piece \#1} \\
 b = \text{piece \#2} \\
 a + b = 150 \\
 a = 2b - 3 \\
 2b - 3 + b = 150 \\
 3b = 153 \\
 b = 51 \text{ yds} \\
 a + 51 = 150 \\
 -51 \quad -51 \\
 \hline
 a = 99 \text{ yds}
 \end{array}$$

Pick a method. Solve these.

$$\begin{array}{l}
 1. \begin{cases} 2y = x + 2 \\ -\frac{1}{2}x + y = 1 \end{cases} \\
 \frac{2y}{2} = \frac{x+2}{2} \\
 y = \frac{1}{2}x + 1 \\
 -\frac{1}{2}x + \frac{1}{2}x + 1 = 1 \\
 1 = 1 \\
 \text{infinitely many}
 \end{array}$$

$$\begin{array}{l}
 2. \begin{cases} y = x - 1 \\ -x + y = 4 \end{cases} \\
 -x + x - 1 = 4 \\
 -1 = 4 \\
 \text{No Solution}
 \end{array}$$

3. Write the following in slope intercept form. Based on the slope, determine if the equations have no solution, 1 solution or infinitely many solutions.

$$\begin{array}{l}
 a. \begin{cases} 3x - 4y = 13 \\ y = -3x - 7 \end{cases} \\
 3x - 4y = 13 \\
 -3x \quad -3x \\
 \hline
 -4y = -3x + 13 \\
 \frac{-4y}{-4} = \frac{-3x + 13}{-4} \\
 y = \frac{3}{4}x - \frac{13}{4} \\
 \text{1 solution}
 \end{array}$$

$$\begin{array}{l}
 b. \begin{cases} 0.5x - y = 30 \\ -0.5x - y = -30 \end{cases} \\
 -y = -0.5x + 30 \\
 -y = -0.5x - 30 \\
 \hline
 0 = 60 \\
 \text{No Solution}
 \end{array}$$

$$\begin{array}{l}
 c. \begin{cases} 3x - 3y = 3 \\ y - y = 1 \end{cases} \\
 3x - 3y = 3 \\
 -3y = -3x + 3 \\
 \frac{-3y}{-3} = \frac{-3x + 3}{-3} \\
 y = x - 1 \\
 \text{Infinitely many}
 \end{array}$$

4. Given the following system of inequalities, find the point(s) that work (are solutions) to the system. Show your work.

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 $y \leq 3x - 5$
 $y \geq x + 2$
 -10

a. (6, 10)
 $10 \leq 3(6) - 5$
 $10 \leq 13 \checkmark$
 $10 \geq 6 + 2$
 $10 \geq 8 \checkmark$

b. (1, 4)
 $4 \leq 3(1) - 5$
 $4 \leq -2 \times$

c. (8, 15)
 $15 \leq 3(8) - 5$
 $15 \leq 19 \checkmark$
 $15 \geq 8 + 2$
 $15 \geq 10 \checkmark$

$15 \geq 15$

$15 > 15$

$9 \leq 15$

$9 < 15$

$-4 > -3$

$-4 \leq -3$

$-900 < -200$

$-9 \geq -2$

$10 \leq 11$

$0 < 10$

$12 \geq 12$

$0 > -12$