

Warmup

Factor the following:

① $7x^2 - 31x - 20$

-140
 $4 \wedge -35$
 $(7x+4)(x-5)$

| | | |
|------|--------|-------|
| | $7x$ | 4 |
| x | $7x^2$ | $4x$ |
| -5 | $35x$ | -20 |

② $4x^2 - 169$
 $2x \wedge 2x$ $-13 \wedge 13$

$(2x+13)(2x-13)$

③ $\frac{3x^2 - 15x - 42}{3}$

$3(x^2 - 5x - 14)$
 $(x-7)(x+2)$
 $x \wedge -7$ $x \wedge -2$

Find the roots (set = 0 and solve)

④ $3x^2 + 2 = 5x$
 $-5x$ $-5x$

$3x^2 - 5x + 2 = 0$

6
 $-2 \wedge -3$

| | | |
|------|--------|-------|
| | $3x$ | -2 |
| x | $3x^2$ | $-2x$ |
| -1 | $-3x$ | 2 |

$(3x-2)(x-1) = 0$

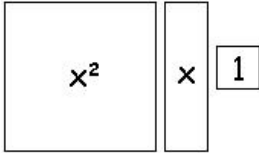
⑤ $x^2 - 81 = 0$
 $x \wedge x$ $-9 \wedge 9$

$(x-9)(x+9) = 0$

$x-9=0$ $x+9=0$
 $+9$ $+9$ -9 -9

$x=9$ $x=-9$

We are going to use the following "tiles" below to help us understand complete the square. Use your imagination.



1.) Review factoring with the following problems.

A.) $x^2 + 2x + 1$
 $(x+1)(x+1)$

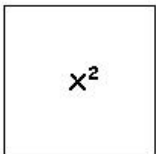
B.) $x^2 + 4x + 4$
 $(x+2)(x+2)$

C.) $x^2 + 6x + 9$
 $(x+3)(x+3)$
 $(x+3)^2$

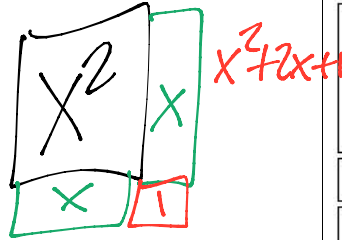
D.) $x^2 + 8x + 16$
 $(x+4)(x+4)$

* Perfect Square Trinomials

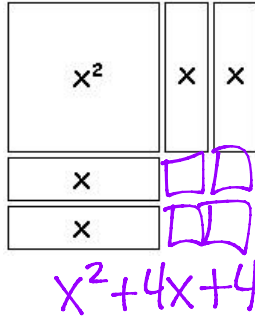
2.) x^2 is already a complete square. You can see that represented with algebra tiles. (what makes this)



3.) $x^2 + 2x$ isn't a complete square. How much do we need to add to it to "complete" it?



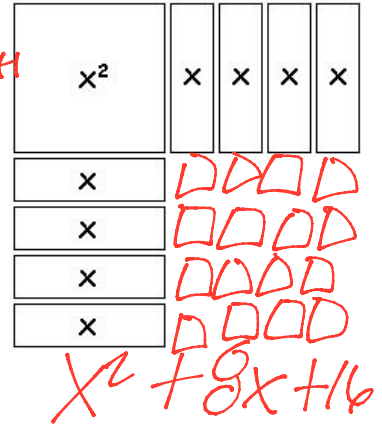
4.) $x^2 + 4x$ isn't a complete square. How much do we need to add to it to "complete" it?



5.) $x^2 + 6x$ isn't a complete square. How much do we need to add to it to "complete" it?



6.) $x^2 + 8x$ isn't a complete square. How much do we need to add to it to "complete" it?



7.) Have you found a pattern yet?

$\frac{1}{2}b$ term
 square # to get
 C

8.) Complete the squares:

$x^2 + 10x + 25$ $x^2 + 14x + 49$
 $\frac{2}{2}$ $\frac{2}{2}$ $(5)^2 = 25$ $(7)^2 = 49$

$x^2 + 3x + 2.25$ $x^2 + \frac{6x}{2} + \frac{9}{4}$
 $\frac{2}{2}$ $(1.5)^2 = 2.25$ $(\frac{b}{2})^2 = \frac{b^2}{4}$

$x^2 + 4x + \frac{4^2}{4}$
 $x^2 + 4x + 4$

Practice completing the square.

$$\frac{x^2 - 14x + \frac{49}{2}}{2} \quad (-7)^2 = 49$$

$$\frac{x^2 - 12x + \frac{36}{2}}{2} \quad (-6)^2 = 36$$

$$\frac{x^2 + 4x + \frac{4}{2}}{2} \quad (2)^2 = 4$$

$$\frac{x^2 - 9x + \frac{20.25}{2}}{2} \quad (-4.5)^2 = 20.25$$

$$\frac{x^2 + 20x + \frac{100}{2}}{2} \quad (10)^2 = 100$$

$$\frac{x^2 - 30x + \frac{225}{2}}{2} \quad (-15)^2 = 225$$

$$\frac{x^2 - 11x + \frac{30.25}{2}}{2} \quad (-5.5)^2 = 30.25$$

$$\frac{x^2 - 15x + \frac{56.25}{2}}{2} \quad (-7.5)^2 = 56.25$$

$$\frac{x^2 + x + \frac{0.25}{2}}{2} \quad \left(\frac{1}{2}\right)^2 = 0.25$$

***Cannot complete the square until A=1**

Before you divide the middle term by 2, you need to take out the GCF. For these, it is ONLY going to be a NUMBER.

Let's do the first one to show you how to complete the rest.

$$\frac{2x^2 - 4x + \frac{1}{2}}{2}$$

* $2 \left(\frac{x^2 - 2x + \frac{1}{2}}{2} \right)$

$2(x-1)(x-1)$

$$\frac{5x^2 + 20x + \frac{4}{5}}{5}$$

$5 \left(\frac{x^2 + 4x + \frac{4}{5}}{5} \right)$

$(2)^2 = 4$

$$\frac{3x^2 - 15x + \frac{6.25}{3}}{3}$$

$3 \left(\frac{x^2 - 5x + \frac{6.25}{3}}{3} \right)$

$(-2.5)^2 = 6.25$

$$\frac{4x^2 - 24x + \frac{9}{4}}{4}$$

$4 \left(\frac{x^2 - 6x + \frac{9}{4}}{4} \right)$

$(-3)^2 = 9$

$$\frac{10x^2 + 10x + \frac{0.25}{10}}{10}$$

$10 \left(\frac{x^2 + x + \frac{0.25}{10}}{10} \right)$

$\left(\frac{1}{2}\right)^2 = 0.25$