

Grab a computer - login and go to web browser to Desmos

GSE Algebra 1

7.1 - Notes

Name: _____

The goal here to see what happens to parabolas as we move them around a graph, what happens in the equation and how that can affect the tables.

Let's look at quadratics again. What shape do they make? parabola

Match the correct statement to the description below.

| Matching Equation (A, B, C, or D) | Statement | Function Equation |
|-----------------------------------|---------------------------------------------------------------|----------------------|
| B | The length of each side of a square is increased by 5 units. | A $A(x) = 5x^2$ |
| C | The length of each side of a square is multiplied by 5 units. | B $A(x) = (x + 5)^2$ |
| D | The area of a square is increased by 5 square units. | C $A(x) = (5x)^2$ |
| A | The <u>area</u> of a square is multiplied by 5. | D $A(x) = x^2 + 5$ |

What is the domain of $y = x^2$? $(-\infty, \infty)$

PARENT FUNCTION: $y = x^2$

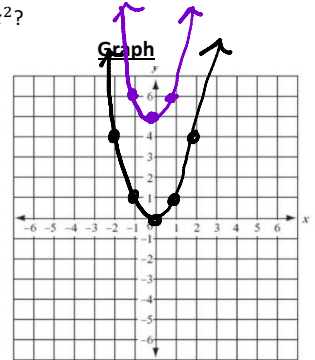
Let's look at how each part above changes the graph, equation and table.

$y = x^2 + 5$

How has this changed from the parent function $y = x^2$?

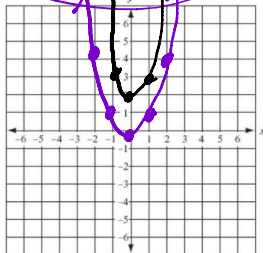
| Equation | |
|--------------|-----------------|
| $y = x^2$ | $y = x^2 + 5$ |
| Parent graph | Move up 5 units |

| Table | | +5 | |
|-----------|---|---------------|----|
| $y = x^2$ | | $y = x^2 + 5$ | |
| x | y | x | y |
| -2 | 4 | -2 | 9 |
| -1 | 1 | -1 | 6 |
| 0 | 0 | 0 | 5 |
| 1 | 1 | 1 | 6 |
| 2 | 4 | 2 | 9 |
| 3 | 9 | 3 | 14 |



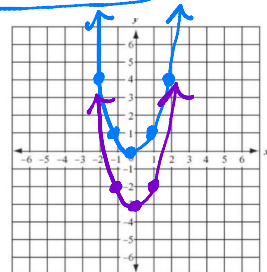
Let's look at a few more. Try these two based off the work from above.

a) $y = x^2 + 2$ UP 2



So the number **OUTSIDE** of the parentheses (in the back of the equation) makes the parabola move UP or Down

b) $y = x^2 - 3$ Down 3



Now let's try this one:

$$x + 5 = 0$$

$$-5 - 5$$

$$x = -5$$

$$y = (x + 5)^2$$

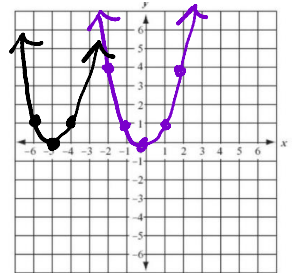
Equation

| $y = x^2$ | $y = (x + 5)^2$ |
|-----------|-----------------|
| | Left 5 |

Table

| $y = x^2$ | | $y = (x + 5)^2$ | |
|-----------|---|-----------------|---|
| x | y | x | y |
| -2 | 4 | -7 | 4 |
| -1 | 1 | -6 | 1 |
| 0 | 0 | -5 | 0 |
| 1 | 1 | -4 | 1 |
| 2 | 4 | -3 | 4 |
| 3 | 9 | -2 | 9 |

Graph



Let's look at a few more. Try these two based off the work from above.

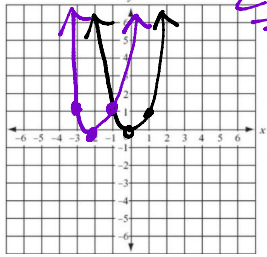
a) $y = (x + 2)^2$

2 left

*only inside ()

b) $y = (x - 3)^2$

Right 3

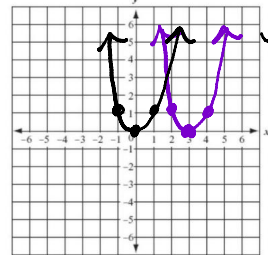


So the number **INSIDE** of the parentheses

(in the middle of the equation) makes the

parabola move left or right

*opposite of sign



Now this one:

$$y = 5x^2$$

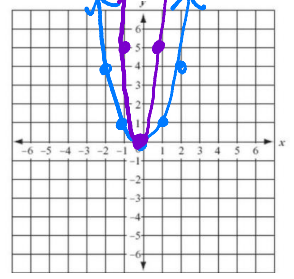
Equation

| $y = x^2$ | $y = 5x^2$ |
|-----------|--------------------------------------------------------|
| | Skinny *Vertical stretch *Horizontal compression |

Table

| $y = x^2$ | | $y = 5x^2$ | |
|-----------|---|------------|----|
| x | y | x | y |
| -2 | 4 | -2 | 20 |
| -1 | 1 | -1 | 5 |
| 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 5 |
| 2 | 4 | 2 | 20 |
| 3 | 9 | 3 | 45 |

Graph



Now try these two:

a) $y = \frac{1}{4}x^2$

| x | -2 | -1 | 0 | 1 | 2 | 3 |
|---|----|------|---|------|---|------|
| y | 1 | 0.25 | 0 | 0.25 | 1 | 2.25 |

fat

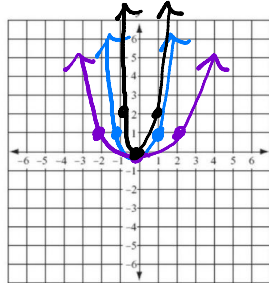
*Horizontal stretch

*Vertically compressed

$$\frac{1}{4}(-2)^2$$

*If your # in front greater than 1 \rightarrow V. stretch

*If your # in front less than 1 (Fraction) \rightarrow H. stretch



b) $y = 2x^2$

skinny

| x | -2 | -1 | 0 | 1 | 2 | 3 |
|---|----|----|---|---|---|----|
| y | 8 | 2 | 0 | 2 | 8 | 18 |

*Vertical stretch

*Horiz. compression

$$2(-2)^2 \quad 2(-1)^2$$

\rightarrow H. stretch

Let's look at what happens when the parabola is flipped upside down.

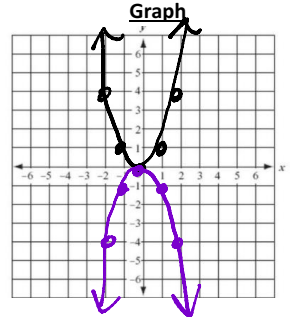
$$y = -x^2$$

Equation

| | |
|-----------|--------------------------------------------|
| $y = x^2$ | $y = -x^2$ |
| | Upside down ↓ ↓ Reflection x-axis |

Table

| $y = x^2$ | | $y = -x^2$ | |
|-----------|---|------------|----|
| x | y | x | y |
| -2 | 4 | -2 | -4 |
| -1 | 1 | -1 | -1 |
| 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | -1 |
| 2 | 4 | 2 | -4 |
| 3 | 9 | 3 | -9 |



So what happens when the number in front of the x^2 is negative?

This is called a Reflection over the x-axis.

Bringing it ALL together!

The vertex form of a quadratic is all of what you just did put together.

$$y = a(x - h)^2 + k \rightarrow \text{Vertex Form}$$

Vertex: (h, k)

What does each part mean?

| | | | | |
|----------|---------------------------------------------------------------|----------------------------------------------------|----------------------------------------------------------------|---------------------------------------------------------------------|
| a | If a is positive ↑ ↑ Face up | If a is negative ↓ ↓ Reflect over x-axis | If $a > 1$ $6x^2$ V. stretch H. compress. | If $0 < a < 1$ $\frac{1}{3}x^2$ Horiz. stretch V. compress |
| h | If h is positive in the equation * $(x+7)^2$ left 7 | | If h is negative in the equation * $(x-4)^2$ Right 4 | |
| k | If k is positive in the equation x^2+2 up 2 | | If k is negative in the equation x^2-14 Down 14 | |

Tell what has happened just based on the equation.

1) $y = 4(x-1)^2 + 3$
 Vert stretch, Right 1, up 3

2) $y = -(x+3)^2 - 2$
 Reflection, Down 2, left 3

3) $y = \frac{1}{3}x^2 - 3$
 H. stretch, V. Compress, Down 3

4) $y = -10(x+2)^2$
 V. stretch, Reflection, left 2

Let's finish these from yesterday